# Robust Hand Detection in Still Video Images Using a Combination of Salient Regions and Color Cues for Interaction with an Intelligent Environment

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The "intelligence" of an intelligent environment is not only influenced by the functionality it offers, but also largely by the naturalness and intuitiveness of its interaction modes. A very important natural interaction mode are gestures, as long as the environment's interface poses no strict constraints on how the gestures may be performed. Since gestures are generally defined by hand/arm poses and motions, an important prerequisite to the recognition of unconstrained gestures is the robust detection of hands in video images. However, due to the strongly articulated nature of hands and the challenges given by a realistic (i.e not strictly controlled) environment, this is a very challenging task, because it means hands need to be found in almost arbitrary configurations and under strongly varying lighting conditions. In this article, we present an approach to hand detection in the context of an intelligent house using a fusion of structural cues and color information. We first describe our detection algorithm using scale-invariant salient region features, combined with an efficient region-based filtering approach to reduce the number of false positives. The results are fused with the output of a skin color classifier. A detailed experimental evaluation on realistic data, including different cue fusing schemes, is presented. By means of an experimental evaluation on a challenging task we demonstrate that, although each of the two different feature types (image structure and color) has drawbacks, their combination yields promising results for robust hand detection.

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#### I. INTRODUCTION

Recent developments of sophisticated pattern recognition techniques nowadays make even the complex analysis of perception related sensor data manageable. In combination with the meanwhile (almost) ubiquitous availability of powerful computing hardware, intelligent technical systems become possible allowing for more intuitive and, thus, natural human-machine interaction (HMI). It is the focus of such systems to be oriented towards the particular users' needs and desires instead towards technical limitations.

But what makes humans perceive a related technical system *intelligent*? An interaction partner is considered as smart if humans may interact with him in the way they normally would with other humans, and he shows reasonable reactions to their actions. So, an *intelligent* system is not only defined by the services it offers (however useful they may be), but also – and more importantly – by the naturalness of interfaces it offers to access these services. Consequently, human-machine interfaces are sought that resemble natural means of human-human communication.

The key modalities used by humans during interaction in the abovementioned "natural" way are speech and gestures. If a person is able to interact with a particular technical system by talking to it and, especially, articulating supporting gestures, the overall communication will appear more natural and, consequently, much easier to the human. Gestures are usually directly connected to acoustic utterances w.r.t. their temporal occurrences. Dynamic gestures are frequently used as some kind of "illustration" of the particular utterances or even without any special contextual relations to the particular interaction. The most prominent use of gestures is, however, their application as illustrating pointing signs. In our work we concentrate on the analysis of gestures belonging to the latter type, e.g. for controlling certain components of electrical equipment included in typical households (lights or sun-blinds).

Since gestures are mostly defined by hand/arm poses and motions, a fundamental prerequisite to their recognition is the robust detection of hands in images. This paper addresses this fundamental stage of gesture recognition especially focusing on unconstrained gestures recorded in (almost) arbitrary environments.

An obvious approach to hand detection corresponds to the detection of skin-color like regions within images of a scene. Especially in office like environments (with furniture which often has skin-like coloring) the exclusive exploitation of such a color cue, unfortunately, results in a (very) large number of false positive predictions.

We developed an appearance-based approach to hand detection using scale-invariant salient region features (cf. [1] for an earlier version). Their evaluation appears promising since a pixel is considered as belonging to a hand only if it resides in a *structurally* "handlike" environment. The approach shows promising results, but still suffers from a rather large number of false positives. Thus, we furthermore focus on improving the robustness of this image-structure based approach by integrating the aforementioned skin color information. The motivation for this is to take advantage of the fusion of two different image cues. Additionally, different fusion techniques are evaluated for the combination of both sources of information for reliable hand detection.

#### A. The FINCA

As an integration scenario of general pattern recognition techniques for intelligent multimodal human-machine interaction in dynamic environments – including gesture recognition based on the hand detection approach described in this article – we are developing an "Intelligent House" – the so-called *FINCA* (a *F*lexible *I*ntelligent e*N*vironment with *C*omputational *A*ugmentation) [2]. The house is integrated into our laboratory at the Robotics Research Institute of Technische Universität Dortmund. Basically, the FINCA integrates two areas under one roof: a smart conference room and, connected to this, an open and flexible labspace. Within both areas various sensors, namely cameras, microphones, infra-red sensors etc. are integrated. Electro-mechanical sensors (e.g. light switches) and actuators (e.g. light or sunblind control units) are integrated and connected via an EIB (European Installation Bus) installation. It is the most intuitive control of these devices we are aiming at, especially using gesture recognition techniques whose pre-requisites are described in this article.

Ultimately an intelligent, cooperative house environment including service robots, which supports human users during various activities (conferences, information retrieval, communication, entertainment etc.), is created. For natural and thus intuitive interaction with the house, special teaching of human users will not be required. Therefore, the FINCA detects, locates and tracks communication partners by analyzing visual and acoustic data. The results are integrated allowing for multimodal scene analysis aiming at a successful automatic interpretation of the user's intentions.

In addition to its role as integration framework for various pattern recognition techniques developed at the Robotics Research Institute, the FINCA serves as a platform for scientific cooperations between researchers from different fields as well as between academia and industry.

Figure 1 gives an overview of the FINCA. On the upper left the house as a whole including our mobile robot is shown. The second image illustrates a typical (multi-modal) interaction scenario within FINCA's smart conference room. All experimental evaluations described in this article have been performed within the FINCA environment.

[Figure 1 about here.]

#### B. Structure of the Article

The remainder of this article is organized as follows. In the subsequent section the related work is briefly reviewed. Descriptions of current techniques for detecting hands in video images – *the* pre-requisite for gesture recognition – are given including both structural and color cues as addressed by this article. In section III the proposed hand detection approach integrating structural and color cues is discussed in detail. We give overviews of our techniques for hand detection with SIFT and skin color classification, respectively. Furthermore, the integration of both cues by sensor fusion is presented. Section IV contains the description of the experimental evaluation we performed demonstrating the effectiveness of the proposed approach.

#### II. RELATED WORK

Many different approaches to hand and limb detection using different kinds of visual cues have been proposed in recent years. A straightforward and simple approach that is often utilized (e.g. [3–5]) is to look for skin-colored regions in the image. Often, simple static color representations by histograms or mixture models (see e.g. [6]) are used. Although this is practicable and efficient given controlled (or known) lighting conditions, skin color classification is difficult to handle under changing illumination. Color is directly influenced by the lighting conditions of the scene and is also dependent on the image acquisition hardware that is used. Thus, a color model that works fine for a given scenario may fail

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when the conditions change. Also, the choice of color space will normally have an effect on classification performance [7]. Instinctively, one would argue that a color space that has some invariance against intensity changes, i.e. that separates the color value from its brightness, would help to overcome some of the problems mentioned above. However, in [8] it is shown that this actually has only minor effects on the model quality and does not solve the general problem.

In order to deal with the difficulties of color classification in dynamic environments several approaches to model adaptation have been proposed. This means the model parameters are adapted automatically to the current lighting conditions, as e.g. in [9–11]. To achieve this, some kind of knowledge of the scene or the current lighting must be inferred from the images. Generally, the problem of model adaptation is not straightforward (for a recent related survey, see e.g. [12]).

An obvious drawback of skin color classification is that other objects having skin-like colors in the chosen representation cannot be differentiated from real skin, and therefore will yield false detections. So, given mostly unconstrained real-world scenarios, skin-color detection seems not reliable enough to be used as a stand-alone cue for hand detection.

Another widely used detection approach is to model an object by its shape, boundaries or general appearance, i.e based on image structure. Well-known examples are the appearancebased object detector of Viola and Jones [13], or Cootes' and Taylor's active appearance models [14]. However, for strongly articulated objects – like hands – showing a large variety of shapes, this is not feasible. Describing all possible appearances of a hand as a whole would either require a very flexible model (which very likely will be too general to be still reliable) or a huge model database that would be very difficult to handle. To overcome this difficulty when dealing with hand gestures, the amount of valid gestures is often limited to a rather small set of predefined poses (e.g. [4, 5]). Effectively, this means reducing the problem of unconstrained gestural interaction to recognition of a gestural command alphabet or sign language. In our research, however, we want the gestural interaction to be as unconstrained and natural as possible, which also implies that untrained users should be able to interact intuitively. Clearly, this is not the case if a command alphabet is defined, because a user has to be instructed which gestures are meaningful.

A possible solution to this problem is given by "part models", as proposed e.g. by Burl et al. [15]. This approach seems more promising for the task of structure-based hand detection

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since it models the object as a set of small characteristic parts (or image regions). The key assumption is that the local appearance of these parts will not change dramatically if the object is deformed or transformed. Thus, if the object is modeled as an assembly of regions (and some weak assumptions on spatial relationships are fulfilled), it may still be identified even under considerable deformations or changes in viewpoint. Another advantage is that partial occlusions of an object can be handled easily, since not all regions must be present to detect an object. As long as a sufficient number of parts can be found and several of them are spatially close, it can be concluded that the particular image area contains the object with high probability.

This leaves the question how to identify "characteristic parts" of the object and how to detect them in an image. A straightforward technique is to use standard appearancebased detectors (like the ones mentioned above) for the separate model parts and then judge the outcome (or find the best combination) by applying the shape constraints. The main drawback of this approach is that it needs to be analyzed in advance which parts of the object are characteristic *and* are big and salient enough to be detected reliably. It would be more feasible to find them automatically, i.e. to apply a salient local feature detection algorithm.

Several salient feature detectors and local region descriptors (i.e. local features) have been proposed. To find objects in arbitrary configurations, they should be invariant to changes in position, scale and rotation of the object they describe. Furthermore, some invariance against affine distortions and illumination changes is required for realistic scenes. The best-known approach to this problem is probably the Harris corner detector [16] – which, however, is not scale invariant. More recent approaches include the salient regions detector of Kadir and Brady [17], the Speeded Up Robust Features (SURF) proposed by Bay et al. [18], and Lowe's Scale Invariant Feature Transform (SIFT) [19].

Given different types of cues, the task is to combine them into an overall classification scheme. A simple yet powerful approach is to concatenate the features into a higherdimensional feature vector and treat them as one. Another possibility is to determine the classification results for each feature separately and then use majority voting or fuse the results on a higher level. For this multi-cue fusion, a great number of general approaches exist, the most straightforward of which are linear combiners (weighted sum, simple and weighted average) [20]. These are, however, only applicable if the results that should be

combined are from the same domain, have the same dimensionality, and are normalized to the same dynamic range. Also, the weights have to be chosen in advance, which is often not straightforward.

Therefore, several approaches deal with learning the weights, or with determining them automatically during run-time. For a comparison of linear combiners vs. common trained fusion rules, see [21]. A more complex dynamic combination scheme called Democratic Integration was proposed by Triesch and von der Malsburg [22]. Martin et al. [23] use Covariance Intersection to fuse detection results from different sensory inputs. Examples for the combination of different cues for hand detection are given in [24] (color and motion cues) and [25] (skin color and appearance-based body parts detector).

## III. HAND DETECTION USING A COMBINATION OF SIFT AND COLOR FEATURES

In the following, we first describe the underlying parts of the classification approach, namely structural detection using SIFT, and skin color based filtering using Gaussian Mixture Models (GMM). Following this, the integration of both parts into a single classifier system is presented.

#### A. Hand detection with SIFT

In section II we stated that, while modeling hands as a whole using their appearance is bound to fail because of their strongly articulated nature, treating them as being composed from small characteristic parts is a promising approach. The question is now how to identify and detect such characteristic parts. We choose to use local descriptors that are computed at automatically determined salient feature points (often referred to as keypoints). In the work presented here, we use the SIFT approach to extract structural features from the camera images. This is mainly because the method is well-known and its potential has been shown in a number of different application fields (e.g. robot self-localization [26], camera calibration and scene reconstruction [27], and object-class recognition [28]). However, the local feature extraction routine for our approach may generally be chosen arbitrarily. We will give only a very brief overview of the SIFT algorithm (for details cf. [19]).

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#### 1. Feature extraction

SIFT is a staged approach, the first stage being the detection of salient keypoints. Keypoint candidates are detected as local extrema of Difference-of-Gaussian (DoG) filters in a Gaussian Scale Space of the input image. These candidates are then sub-pixel interpolated. Keypoints showing low contrast or lying on edges are discarded, for they are not stable.

Invariance against scale and rotation is achieved by assigning a scale (according to the level of the scale space pyramid the keypoint was detected in) and an orientation (according to the principal orientation of gradients in a region around the keypoint) to each keypoint. Note that in this step, points may be duplicated with different orientations if the local orientation histogram has multiple prominent peaks.

Finally, the local image descriptor (i.e. the features) is calculated as a collection of smoothed histograms of gradient orientations and magnitudes over the local image region. The size of the feature vector depends on the number of histograms and the number of bins in each histogram. In Lowe's original implementation, a 4-by-4 patch of histograms with 8 bins each is used, yielding a 128-dimensional feature vector. We use a MATLAB/C implementation of the SIFT algorithm provided by Andrea Vedaldi [29].

#### 2. Matching

Given an image of the scene, we obtain a (typically large) number of SIFT features describing salient points in the image. In order to detect hands, we build a database containing descriptors extracted from many images containing hands in different configurations (see section IV A for details on the data). We also build a large database of background descriptors from images taken inside the FINCA. Following Lowe's proposal for object recognition, we implement the matching algorithm as follows: Let  $k_i$  be the keypoint descriptor that should be classified. Let  $d_{fg}$  and  $d_{bg}$  be the Euclidean distances to the nearest neighbors (found by means of a kd-tree [30] search) to  $k_i$  from the foreground and background databases, respectively. We decide on the keypoint being fore- or background by thresholding the classification score  $s_{class}$ , which is the ratio of the two distances  $d_{fg}$  and  $d_{bg}$ .

#### 3. Candidate filtering

With the above matching process, we obtain a label for each keypoint in the input image. To achieve a high number of true positives, we have to choose a classification threshold  $t_{class}$  on  $s_{class}$  that is larger than 1, i.e. we actually allow for keypoints to be classified as positives even if a slightly better match has been found in the background database. Obviously, this results in a large number of false positives, a drawback that has also been reported by Lowe for matching on keypoint level. This is why Lowe suggests matching groups of features using a generalized Hough transform followed by a detailed geometric fit [19]. While this yields excellent results for rigid object detection, it is not applicable to the problem of hand detection, again due to the strongly articulated nature of hands and because we expect to see them in arbitrary configurations and viewing angles. We have to apply a weaker constraint on spatial configuration.

Because SIFT yields a large number of keypoints (around 1 000 for a typical image from our sample set), we assume that typically we will find multiple keypoints on hands of which most will be classified as foreground (i.e. we have a low false negative rate) whereas most false positives will be scattered over the image and thus will be surrounded by numerous true negatives. In other words, we expect the true positives to form spatial clusters while false positives will often be isolated, and consequently use this as constraint to eliminate false positives. This leads to an efficient candidate filtering algorithm by analyzing lists of keypoints spatially connected to the candidates in question. The outline of the algorithm is given in figure 2.

## [Figure 2 about here.]

The first step is to determine the adjacency list for each (positive) keypoint candidate. Three different approaches were implemented and evaluated: Circular regions of fixed size centered around the candidate; circular regions with sizes proportional to the SIFT scale of the candidate; and taking the n spatially nearest neighbors. We then evaluate points based on the total number of positive candidates in their respective list (threshold  $n_{pos,min}$ ) and the ratio between positives and negatives (threshold  $f_{min}$ ). If a candidate passes both criteria, it is accepted as foreground point. If it fails on both criteria, it is rejected. Otherwise, it is further evaluated in a second step by determining the number of positives m it is connected to.

This approach discards a large number of false positives and yields promising results. Still, however, it cannot handle clusters of false positives and fails to reject them. Figure 3 shows two example results.

[Figure 3 about here.]

#### B. Skin color classification

Since most approaches relying on a single type of feature exhibit drawbacks in specific fields or under certain circumstances, it is intuitive to think about the integration of different features. Provided that the different cues show substantially different characteristics and behavior, the assumption is that the strengths of one of them can compensate for the weaknesses of others, and vice versa. Consequently, this should yield a system that shows better results, reliability and robustness than any of the respective subsystems. In our scenario, we have a structure-based region classifier for hand detection that typically suffers from a large number of false positives (cf. section III A). Despite the drawbacks of skin color detection (as discussed in section II), it seems reasonable to utilize a skin-color classifier because it will reliably reject those false positives that lie on non skin-colored regions. Plus, a non-adaptive color model may be implemented as a simple look-up table once it has been trained, and thus adds almost no additional computational costs. However, the answer to the question how the different features should be combined to achieve the best result is, in general, not straightforward. In section III C, we will investigate different alternatives.

For the purpose of skin color detection, we utilize a simple approach using Gaussian Mixture Models (GMMs): The training samples are first clustered using the k-means algorithm and then the clusters are approximated by Gaussian distributions. The final model thus consists of several multivariate Gaussians representing the sample distribution. Images are classified pixel-wise by calculating the model scores for the pixel color values and then determining the class of the "best" mixture. Obviously, as mentioned above, this can be done by generating a look-up table using a color dummy file.

The models were trained on a small set of training images (see section IVA). Two mixtures were trained separately for fore- and background, respectively, and then combined into a single model. We investigated different color spaces and mixture sizes in order to find the best combination for our data.

Note that in our scenario, the conditions for skin color detection can be very challenging since some cameras directly face the windows (glare effects, with most of the objects in front of the window appearing almost black) and the wood inlay of the furniture has a skin-like color (cf. figure 5). This results – consistently for all tested color spaces – in a rather large error rate for skin pixels, since the background set contains many skin-like samples.

#### C. Data fusion

Given the abovementioned structural and color cues, the task is to combine them into a single classifier system which can be used for robust hand detection in video images. In this article we investigated three different fusion approaches.

A straightforward approach is to incorporate the skin color map computed using GMMs within a pre-processing step. Here, a binary skin map is computed and used to mask the input image. Subimages enclosing non-zero image regions are extracted, and SIFT based hand detection is applied to these subimages only (instead of the whole image). Compared to most other approaches, this has the additional advantage of considerably accelerating the matching process, since large portions of the input image do not have to be treated. Alternatively (but principally identically), fusion can be performed as post-processing where the SIFT keypoints are weighted by their skin color probability.

The second integration approach we considered combines both features in a single (higherdimensional) feature vector prior to classification. This is done as follows: First, we calculate a color histogram over an image region specified by the keypoint scale (meaning we actually do not use the GMM skin classifiers for this approach). This histogram is then vectorized, normalized to unit length and attached to the SIFT descriptor. Classification is performed as described in section III A 2 using the compound feature vector. Of course, the database entries used for NN matching must then be constructed in the same way.

Our third approach incorporates the combination of saliency maps which are calculated separately for both information cues. Every positive keypoint (either SIFT or skin color related) serves as origin of a single Gaussian. For the SIFT saliency map, the variance of the Gaussian is dependent on the particular scale of the SIFT-keypoint. For the skin map, a fixed variance is used. Figure 4 shows an example. The two saliency maps are then fused. The resulting combined map is thresholded and all hand candidates having saliency values below the threshold are rejected.

[Figure 4 about here.]

#### IV. EXPERIMENTAL EVALUATION

In order to evaluate the effectiveness of the new approach for the detection of hands in video images proposed in this article, we conducted various practical experiments. Therefore, human users of our intelligent house (cf. section IA) were asked to perform certain gestures in ordinary situations within the smart conference room of the FINCA. By means of the ceiling-mounted video cameras, still images capturing the gestures were taken and, subsequently, analyzed using the techniques presented in the previous sections.

In the following the results of the experiments are presented in detail. First the datasets used are described. After that results for the SIFT-based detection approach as well as for the combined approach integrating both structural and color cues are given.

#### A. Datasets

For training and testing, we recorded a dataset of 466 color images with PAL resolution. The set was recorded inside our intelligent house using two cameras covering different views of the room over different days and under varying lighting conditions. It contains images of 4 different persons wandering around inside our smart conference room and gesticulating. Note that we did not constrain the type of poses or gestures performed, that the persons appeared in different distances to the cameras, and that they were allowed to move around freely in the camera's field of view. Figure 5 shows some example images.

These images were segmented into hand and non-hand parts manually, where a small region around the perimeter of hands is also labeled as belonging to the hand to account for SIFT descriptors that describe typical hand regions, but lie outside the actual skin area. From this set, 145 images were randomly selected for testing. The remaining 321 images were taken for training of our classifier. GMM-training for skin color classification (section IIIB) was performed on an alternative set of 46 sample images from the same scenario.

The final database of SIFT descriptors applied for the evaluation of the structural cue contains approximately 200 000 entries for the background, and 8 700 for the foreground (i.e. the hands).

[Figure 5 about here.]

#### B. SIFT-based Hand Detection

In the first part of the experimental evaluation we concentrated on the effectiveness of the SIFT-based approach for hand detection in still video images, i.e. the structural cue was used exclusively (cf. also [1]). We, therefore, applied variants of our detection approach as described in section III aiming at the evaluation of the approach in general and of the effectiveness of the proposed rejection criterion, respectively.

Using the database of SIFT descriptors extracted from training images (see previous section), first, the standard nearest neighbor (NN) matching technique (implemented as kd-tree search for speedup) as described in [19] is applied to the set of test images. The goal of this specific evaluation is to investigate whether SIFT descriptors are suitable in general for the detection of articulated objects like hands in unstructured images originating from real world scenarios. Note that SIFT has originally been developed for the detection of rigid, i.e. non-articulated objects in images where those objects known from training samples might occur as scaled or rotated instances. As mentioned before, in our scenario no constraints w.r.t. the appearance of the hands to be detected in the images are given.

The ROC curve for NN matching using the full database of training examples is shown in figure 6, the variational parameter being the threshold  $t_{class}$  on the distance ratio  $s_{class}$ . It can be seen that, generally, the original SIFT approach for rigid object detection using simple NN matching already yields satisfactory results. To get a high number of true positives, we allow for the accepted points to have a distance ratio  $s_{class} > 1.0$ , which means they are in fact more similar to some of the background examples. The point marked with 90% true positives<sup>1</sup> and 6.8% false positives corresponds to a threshold of 1.7. Due to the large number of keypoints that are identified by SIFT (typically 800 - 1600 per image), this results in a large number of false positives which typically lie on foreground objects (e.g. the person's body) not represented in the database. However, a considerable number of these will be discarded by our filtering algorithm.

## [Figure 6 about here.]

 $<sup>^{1}</sup>$  We assume that, for our application, a true positive rate lower than 85 to 90% will not be sufficient.

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By means of the proposed rejection scheme, i.e. the modification of the original SIFTbased detection, the abovementioned reduction of false positive classifications is addressed. As described in section III, this rejection scheme consists of a hyteresis-like approach where a list of keypoints spatially connected to the candidate in question is determined. Based on a two-stage filtering technique, the number of false positives is considerably reduced.

In a set of experiments we evaluated the influence of the three parameters  $n_{pos,min}$ ,  $f_{min}$ and m using different classification thresholds  $t_{class}$  for the NN matching stage and several region sizes. Basically, the algorithm (cf. figure 2) contains three different (technical) definitions of spatial neighborhood resulting in regions

- 1. defined depending on the particular SIFT scale,
- 2. of fixed sized, or
- 3. containing the k nearest neighbors.

By analyzing the particular ROC curves the experimental evaluation turned out that all three variants reduce the number of false positives successfully. Basically, scale-based and fixed regions do not differ substantially w.r.t. the reduction rates, which, on the first hand, seems surprising. Reconsidering the setting of the evaluation, it becomes clear that this behavior seems to be an artifact of the sample set analyzed. The room the images were recorded in is quite small, and so the assumption that hand sizes do not vary strongly holds for most cases. Given a different scenario, a negative effect is very likely when using a fixed region size. Detailed results for the abovementioned variants of determining the particular keypoint lists are given in [1].

The third variant for candidate filtering does not use explicit regions, instead we generate the input list using the k spatially closest keypoints to the candidate. Figure 7 shows the ROC curves for this approach. Compared to the aforementioned definitions of regions surrounding a particular keypoint, our filtering technique analyzing the k nearest neighbors performed best since we do not make assumptions on appropriate region sizes, but evaluate the same number of neighboring points for each candidate.

## [Figure 7 about here.]

Reconsidering the overall algorithm (cf. figure 2) it can be seen that the criteria evaluated so far – the minimum required number of positives  $n_{pos,min}$  and the minimum ratio of

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positives and negatives  $f_{min}$  – both belong to the first stage and are applied simultaneously. However, failing one of them is not sufficient to reject a candidate keypoint. Instead, we only reject keypoints that fail on *both* conditions, and we only accept those that satisfy both. The remaining, which pass one criterion, but fail on the other, are further evaluated in a second stage.

In this second stage of the filtering approach the m spatially closest neighbors of the candidate point are considered. A keypoint is only accepted as true positive if *all* m neighbors are true positives, which means they must all have passed both conditions in the first stage. Setting m to a high value will eliminate "isolated" positives, but will also tend to discard key points at the margins of positive clusters. Figure 8 shows the ROC curves for different parameter combinations, variating m in a reasonable range (from 0 to 10). The plot has been scaled for better recognizability. Note that these curves have two fixed ends that are defined by the outcome of the first filtering stage: The starting point corresponds to the complete set of candidates that passed one of the two initial conditions, the end point to the number of candidates that passed both conditions. It can be seen that this is a pretty strong criterion, since for all values of m > 0, a certain portion of true positives is rejected. However, the effect on false positives is stronger. Since most false positives are already rejected for m = 1, and higher values for m will only discard more true positives, we will only take into consideration values of 1 and 2 for m for the evaluation of our complete system.

## [Figure 8 about here.]

Table I shows the results of a few example runs using parameter sets that seem reasonable based on the aforementioned evaluation results of the different stages. For almost all parameter combinations, the filtering approach achieves a substantial reduction of the number of false positives while retaining true positive rates only slightly lower than in the initial NN matching stage. The best combinations reduce the number of false positives by one half, while only dropping around 5% of the true positives. This is an acceptable tradeoff, since the required rate of approximately 90% true positives can still be achieved in most cases.

[Table 1 about here.]

#### C. Detection of Hands using Cue Integration

In the previous sections it was shown that by means of SIFT-descriptors reliable hand detection in video images of realistic HMI scenarios is possible. We, furthermore, demonstrated that the rather high number of false positive detections as produced when applying the original SIFT approach can substantially be reduced using the proposed hysteresis-like filtering technique.

The basic idea of the hand detection method described in this article is, however, not limited to the exploitation of the structural cue. Instead, color information is integrated aiming at a further reduction of the number of false predictions, which is especially necessary for robust gesture recognition as an intuitive input modality in human-machine interaction applications. Note that the exclusive use of skin-color classification based approaches is, due to the complex setting in our intelligent house environment, not suitable for our scenario.

We trained our skin models on 46 image samples in full PAL-resolution (yielding a total of more than 19.3 Million pixels) recorded within our target scenario. The data was manually labeled with respect to skin color. In summary, the dataset contained 17.7 Million background pixels and 1.6 Million skin pixels. These were used to separately train mixture models for skin and background which were then combined into a single model. Eight different color spaces were investigated, and the number of Gaussians in the models was varied between 5 and 150. We will skip the detailed evaluation results for the whole process (because this would go beyond the scope of this article) and only report the best results that were achieved.

We found the classifiers trained in the L\*a\*b and normalized RG (nRG) color space to work best. For robust detection of skin colored regions a small number of mixtures (L\*a\*b: 5 for skin, 16 for background; nRG: 5/2) was found to be sufficient. On a test data set containing 13 Million pixels, the L\*a\*b\* classifier achieved an overall classification error of 2.8%. While only 0.7% of background pixels were classified incorrectly, the error rate for skin pixels was 53%. For the nRG classifier, the overall error rate was 10%, which, in comparison, is rather high. However, this classifier showed the best results for skin pixels (32% error rate). So, we have two classifiers showing substantially different behavior on the test set: The L\*a\*b\* classifier is "pessimistic", striving for a low overall error rate and accepting a large number of false negatives to achieve this, while the nRG classifier is more "optimistic"

and trades in a good skin recognition rate for a higher number of false positives.

As discussed in section IIIC, different schemes for fusing the data from both the SIFTbased structural cue and the skin-color cue are investigated.

First experiments showed that using binary (morphologically closed) skin maps as preor postprocessing step is not suitable for robust hand detection. This is because many of the structural descriptors that describe hands lie in fact outside the skin area. Also, since a skin color segmentation will never be perfect and will still exhibit holes inside skin areas, some true positives lying on skin will also be discarded. Thus we concentrated on the latter two integration methods.

In figure 9 the results of the evaluation of enhanced SIFT descriptors are presented. We evaluated certain variants for descriptor enhancements using different color space models and granularities of the appropriate histograms, namely HSV (h32 and hs8x8), normalized RG (n-rg8x8), and LAB ((l)a\*b\*8x8). The dimensionality of the original descriptor vectors (128) was enhanced by the particular histogram sizes. It can be seen that, although the integration technique works in principle, only slight improvements over the SIFT-only detection (denoted as kd-tree where the name originates from the actual implementation of the matching technique as a kd-tree) can be achieved. In fact, in some cases the performance got even worse than the reference. The reason for this lies in the missing flexibility of color histograms w.r.t. illumination changes (which are included in the – realistic – sample-set used).

## [Figure 9 about here.]

The third type of fusing both sources of information is based on the integration of saliency maps each calculated separately for the SIFT- and the color-cue, respectively. In order to actually combine the probability maps, basically, different strategies can be used. In our experiments we focused on the pixel-wise (weighted) summation of saliency values.<sup>2</sup> We also tried multiplying the maps which, however, did not improve the results and when using the  $L^*a^*b$  color space produced even worse results. This is mainly reasoned by the fact that in this case multiplying saliency maps suffered from the rather pessimistic behavior of the particular skin classifiers skipping too many true positives.

 $<sup>^2</sup>$  In the experiments described in this paper the particular saliencies were equally weighted.

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In figure 10, ROC curves for the summation of SIFT-based and n-RG based (top), or L\*a\*b based (bottom) skin color saliencies are shown. Again the reference curve representing the results obtained when evaluating SIFT-descriptors only is denoted as kd-tree (see explanation in previous section). For the saliency combination three different curves are given where the SIFT thresholds for NN classification are modified. Analyzing the ROC curves it can be seen that the integration of structural and color cues by combining related saliency maps greatly reduces the number of false positive detections while still very high true positive rates can be achieved.

## [Figure 10 about here.]

To summarize in figure 11 we show the best results for both skin classifiers based on nRG and L\*a\*b color space, respectively. The variational parameter is the classification threshold on the combined saliency map as described earlier. We marked two "working points" with a true positive rate of 90% and 94%. In the first case the false positive rate could be reduced from 6.3% to 4.2% (a relative reduction by 33%) using the L\*a\*b colorspace, and to 4.5% (relative 28%) using nRG. In the latter case the reduction is from 7.5% to 5.0% (33%) and to 5.4% (28%), respectively.

[Figure 11 about here.]

#### V. CONCLUSION

The basic motivation for the development of so-called "intelligent systems" for humanmachine interaction (HMI) applications is to allow for most intuitive and, thus, easy usability of technical systems. Humans usually consider a system as smart if it shows reasonable reactions to their actions related to the services offered. An important aspect for the acceptance and usefulness of such intelligent systems is the naturalness of interfaces it offers.

The key modalities used by humans for "natural" interaction with technical systems are speech and gestures. In order to allow for gesture recognition including both dynamic and static (e.g. pointing) gestures the robust detection of hands in video images is a major prerequisite. In this article we presented an approach for robust hand detection in still video images covering realistic scenarios.

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In our work we, generally, focus on the recognition of unconstrained gestures performed in (almost) arbitrary environments. Due to their rather limited performance for related still video images, especially originating from scenarios with different lighting conditions, standard skin-color classification based approaches for hand detection cannot be used exclusively. Thus, we developed an detection approach which is based on the exploitation of two different sources of information, namely a structural cue and a skin-color cue.

For the structural cue integrated into our overall detection algorithm, SIFT-descriptors are used. This initial classification step is based on a database of descriptors which are trained on sample images containing either hands or background. By means of a hysteresislike filtering technique, the number of false positive classifications can be limited reasonably. In order to further reduce the number of misclassifications, the approach proposed in this article additionally contains a skin-color classification stage based on Gaussian Mixture Models. By means of saliency maps derived from both cues data fusion is performed.

We demonstrated the effectiveness of our approach in a detailed experimental evaluation on a challenging task related to human-machine interaction in our intelligent house, the FINCA. For different lighting conditions, hands could be detected robustly in images covering different views of our smart conference room, where different people were wandering around and gesticulating in an unconstrained manner.

The major outcome of the developments presented in this article and, thus, the main contribution of our work is the realization of an important initial stage for actual gesture recognition. Consequently, intelligent human-machine interaction applications exploiting this intuitive modality in related domains can benefit from the approach presented.

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## Authors' Biographies



Thomas Plötz received the diploma in technical computer science from the University of Cooperative Education Mosbach, Germany, in 1998. He received the diploma and a PhD degree (Dr.-Ing.) in computer science from the University of Bielefeld, Germany, in 2001 and 2005, respectively.

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Dr. Plötz is interested in general aspects of machine learning and pattern recognition techniques and applications for various domains like speech-processing, automatic recognition of handwritten script, image processing or bioinformatics. He is coordinating various research activities within the Smart environment project at the Robotics Research Institute's "Intelligent House" – the FINCA.



**Jan Richarz** received the diploma in computer engineering from the Ilmenau Technical University, Germany, in 2006.

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Gernot A. Fink received the diploma in computer science from the University of Erlangen-Nürnberg, Erlangen, Germany, in 1991 and the Ph.D. degree (Dr.-Ing.) also in computer science from Bielefeld University, Germany, in 1995. In 2002 he received the venia legendi (Habilitation) in applied computer science from the Faculty of Technology of Bielefeld University.

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Dr. Fink is Senior Member of the Institute of Electrical and Electronics Engineers (IEEE), the IEEE Signal Processing Society, and the IEEE Computer Society.

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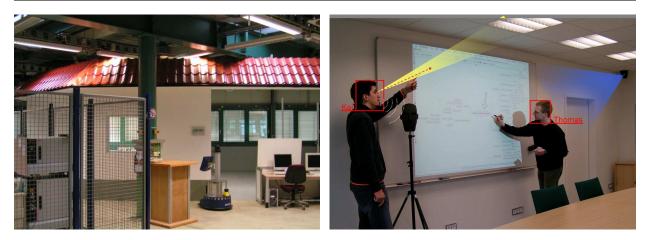


Figure 1: Overview of the integration scenario – an Intelligent House, the FINCA, developed at the Robotics Research Institute of Technische Universität Dortmund (see text for description).

for all keypoints  $k_1...k_n$  labeled as positives do  $list = getKeypointList(k_i)$ count positives  $n_{pos}$  and negatives  $n_{neg}$  in listif  $(n_{pos} \ge n_{pos,min})\&(\frac{n_{pos}}{n_{neg}} \ge f_{min})$  then accept  $k_i$  as true positive. else if  $(n_{pos} < n_{pos,min})\&(\frac{n_{pos}}{n_{neg}} < f_{min})$  then reject  $k_i$ else find the m keypoints  $l_1...l_m$  closest to  $k_i$ if  $l_1...l_m$  are all true positives then accept  $k_i$  as true positive else reject  $k_i$ end if end if

end for

**function** getKeypointList(*candidate*)

a) list = all points in circular region around candidate with r = σ · c, c = const, σ = candidate scale
b) list = all point in circular region around candidate with r = c, c = const
c) list = n spatially closest points to candidate

return *list* 

Figure 2: Outline of the candidate filtering algorithm.

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Figure 3: Examples for SIFT based hand detection results. Sift keypoints are depicted by squares, white squares represent positives, black squares are negatives. Left: Very good detection, the hands are identified correctly and almost all false positives are discarded. Right: Here, the filtering algorithm fails because the false positives form large clusters.

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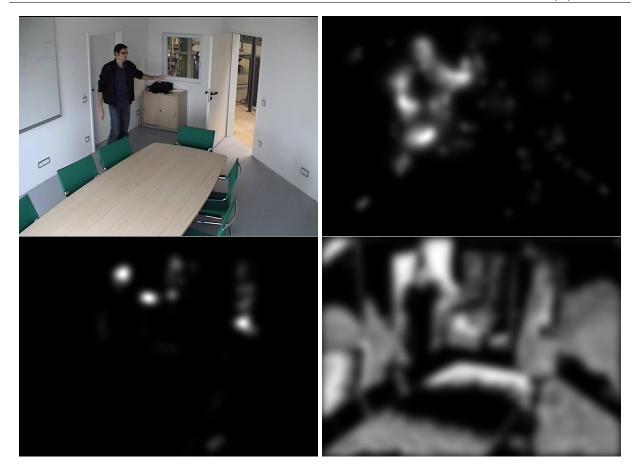


Figure 4: Examples for saliency maps. From left to right, top to bottom: Original image, SIFT saliency, skin saliency (L\*a\*b\* classifier), skin saliency (nRG classifier)



Figure 5: Typical examples of camera images used

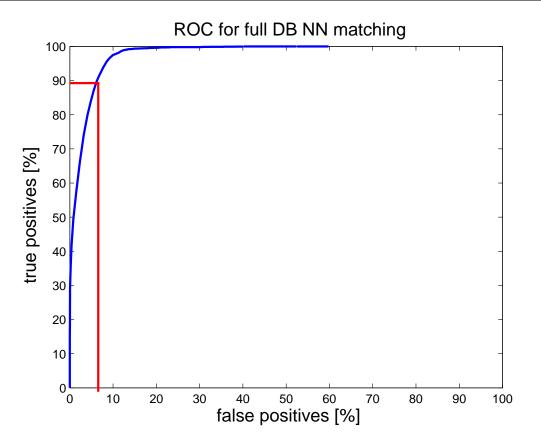


Figure 6: Effectiveness of the exclusive application of the structural cue for hand detection in still video images: The ROC curve illustrates the results for nearest neighbor matching using the complete training database of SIFT descriptors.

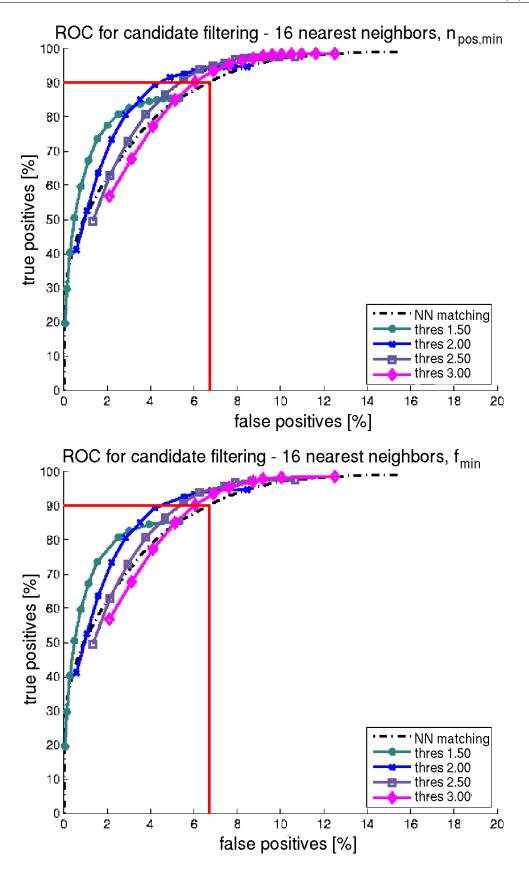


Figure 7: ROC curves for candidate filtering in hand detection applying SIFT only using k = 16 nearest neighbors. Top: Variating  $n_{pos,min}$ . Bottom: Variating  $f_{min}$ .

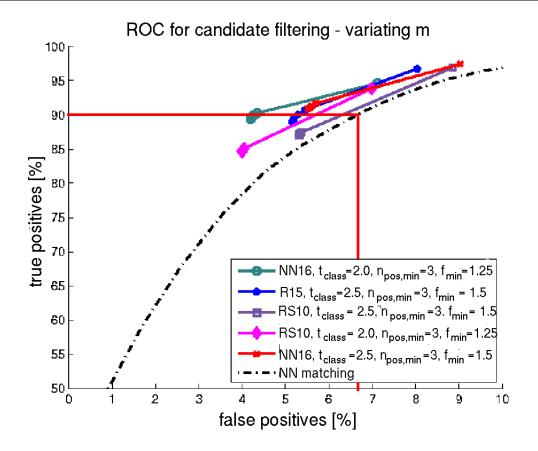


Figure 8: ROC curves for candidate filtering in hand detection applying SIFT only variating m with different parameter sets. NN16: 16 nearest neighbors. R15: fixed region size 15. RS10: region size  $10 \cdot \sigma$ .

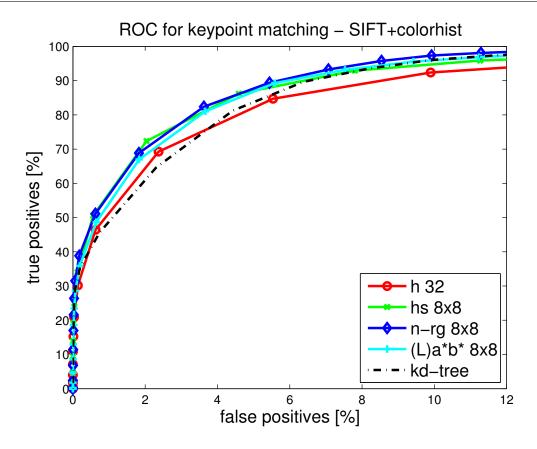


Figure 9: ROC curves for hand detection experiments using enhanced SIFT descriptors additionally integrating color histograms of the particular keypoints' regions. kd-tree: reference using original SIFT descriptors; h32: additional incorporation of hue-based color histograms (from HSV color space) with 32 bins; hs8x8: integrated color histogram is based on hue and saturation (from HSV color space) and calculated on  $8 \times 8$  bins; n-rg8x8: same as hs8x8 but using normalized RG color space; (l)a\*b\*8x8: dito for LAB space.

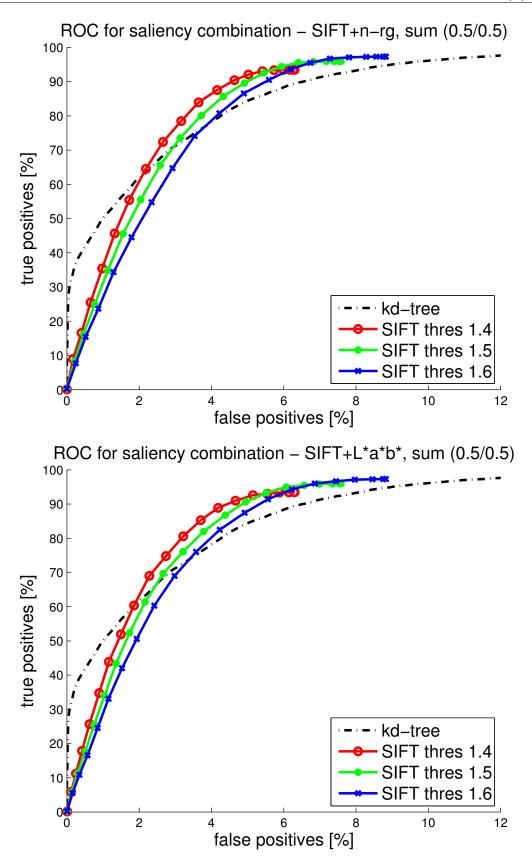


Figure 10: ROC curves illustrating the efficiency of the combined hand detection approach using SIFT and skin color cues integrated by summation of derived saliencies (top: n-RG color space; bottom: L\*a\*b color space used) (© MAIK Nauka/Interperiodica, distributed exclusively by Springer Science+Business Media LLC. Personal use of this material is permitted. However, permission to reprint/republish this material for advertising or promotional purposes or for creating new collective works for resale or redistribution to servers or lists, or to reuse any copyrighted component of this work in other works, must be obtained from the publisher.

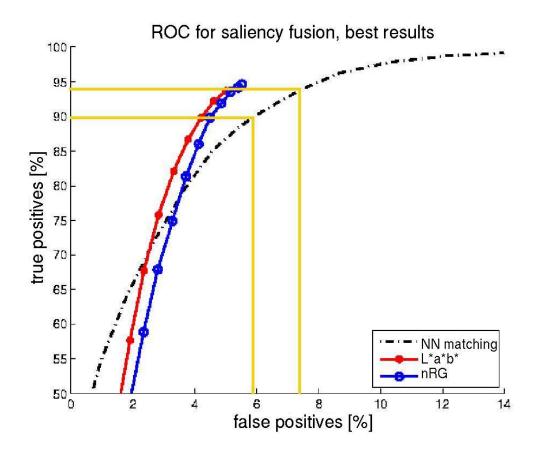


Figure 11: Best results for saliency fusion using  $L^*a^*b$  and nRG(B) color space for skin color classification.

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	region	$t_{class}$	n	$f_{min}$	m	% TP ( $\Delta NN$ )	% FP $(\Delta NN)$
1	RS10	2.0	3	1.25	1	85.08 (-10.2)	4.04(-52.3)
2	RS10	2.5	3	1.00	2	91.55 (-6.2)	6.32 (-40.8)
3	R15	2.0	4	1.25	1	88,18 (-6.9)	4.05 (-52.2)
4	R15	2.5	3	1.00	2	93.07 (-4.6)	6.00 (-43.8)
5	NN16	2.0	4	1.25	1	90.26 (-4.7)	4.34 (-48.8)
6	NN16	2.5	3	1.50	2	91.30 (-6.4)	5.61 (-47.4)

Table I: Some example results using the complete filtering algorithm.  $n_{pos,min}$  abbreviated to n. RS10: region size  $10 \cdot \sigma$ . R15: fixed region size 15. NN16: 16 nearest neighbors. The values in brackets give the relative drop for the true and false positive rates compared to NN matching with the same threshold  $t_{class}$ .